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Zhang, Weijian and Higham, Nicholas J.

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## Matrix Depot: An Extensible Test Matrix Collection for Julia\*

Weijian Zhang and Nicholas J. Higham<sup>†</sup>

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#### Abstract

Matrix Depot is a Julia software package that provides easy access to a large and diverse collection of test matrices. Its novelty is threefold. First, it is extensible by the user, and so can be adapted to include the user's own test problems. In doing so it facilitates experimentation and makes it easier to carry out reproducible research. Second, it amalgamates in a single framework three different types of matrix collections, comprising parametrized test matrices, regularization test problems, and real-life sparse matrix data. Third, it fully exploits the Julia language. It uses multiple dispatch to help provide a simple interface and, in particular, to allow matrices to be generated in any of the numeric data types supported by the language.

Keywords: Julia; software package; test matrices; test problems; matrix algorithm.

#### 1 Introduction

In 1969 Gregory and Karney published a book of test matrices [14]. They stated that "In order to test the accuracy of computer programs for solving numerical problems, one needs numerical examples with known solutions. The aim of this monograph is to provide the reader with suitable examples for testing algorithms for finding the inverses, eigenvalues, and eigenvectors of matrix." At that time it was common for journal papers to be devoted to introducing and analyzing a particular test matrix or class of matrices, examples being the papers of Clement [7] (in the first issue of SIAM Review), Pei [24] (occupying just a quarter of a page), and Gear [13].

Today, test matrices remain of great interest, but not for the same reasons as fifty years ago. Testing accuracy using problems with known solutions is less common because a reference solution correct to machine precision can usually be computed at higher precision without difficulty. The main uses of test matrices nowadays are for exploring the behavior of mathematical quantities (such as eigenvalue bounds) and for measuring the performance of one or more algorithms with respect to accuracy, stability, convergence rate, speed, or robustness.

Various collections of matrices have been made available in software. As well as giving easy access to matrices these collections have the advantage of facilitating reproducibility of experiments [10], whether by the same researcher months later or by different researchers.

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<sup>&</sup>lt;sup>†</sup>School of Mathematics, University of Manchester, Manchester, M13 9PL, England (weijian.zhang@manchester.ac.uk, nick.higham@manchester.ac.uk).

An early collection of parametrizable matrices was given by Higham [20] and made available in MATLAB form. The collection was later extended and distributed as a MATLAB toolbox [21]. Many of the matrices in the toolbox were subsequently incorporated into the MATLAB gallery function. Marques, Vömel, Demmel, and Parlett [23] present test matrices for tridiagonal eigenvalue problems (already recognized as important by Gregory and Karney, who devoted the last chapter of their book to such matrices). The Harwell–Boeing collection of sparse matrices [11] has been widely used, and is incorporated in the University of Florida Sparse Matrix Collection [8], [9], which contains over 2700 matrices from practical applications, including standard and generalized eigenvalue problems from [1]. Among other MATLAB toolboxes we mention the CONTEST toolbox [25], which produces adjacency matrices describing random networks, and the NLEVP collection of nonlinear eigenvalue problems [2].

The purpose of this work is to provide a test matrix collection for Julia [3], [4], a new dynamic programming language for technical computing. The collection, called Matrix Depot, exploits Julia's multiple dispatch features to enable all matrices to be accessed by one simple interface. Moreover, Matrix Depot is extensible. Users can add matrices from the University of Florida Sparse Matrix Collection and Matrix Market; they can code new matrix generators and incorporate them into Matrix Depot; and they can define new groups of matrices that give easy access to subsets of matrices. The matrices can be generated in any appropriate numeric data type, such as

- floating-point types Float16 (half precision: 16 bits), Float32 (single precision: 32 bits), and Float64 (double precision: 64 bits);
- integer types Int32 (signed 32-bit integers), UInt32 (unsigned 32-bit integers), Int64 (signed 64-bit integers), and UInt64 (unsigned 32-bit integers);
- Complex, where the real and imaginary parts are of any Real type (the same for both);
- Rational (ratio of integers); and
- arbitrary precision type BigFloat (with default precision 256 bits), which uses the GNU MPFR Library [12].

This paper is organized as follows. We start by giving a brief demonstration of Matrix Depot in Section 2. Then we explain the design and implementation of Matrix Depot in Section 3, giving details on how multiple dispatch is exploited, how the collection is stored, accessed, and documented, and how it can be extended. In Section 4 we describe the three classes of matrices in Matrix Depot: parametrized test matrices, regularization test problems, and real-life sparse matrix data. Concluding remarks are given in Section 5.

## 2 A Taste of Matrix Depot

To download Matrix Depot, in a Julia REPL (read-eval-print loop) run the command

```
> Pkg.add("MatrixDepot")
```

Then import Matrix Depot into the local scope.

```
> using MatrixDepot
```

Now the package is ready to be used. First, we find out what matrices are in Matrix Depot.

```
> matrixdepot()
Matrices:
                      2) binomial
                                         blur
                                                             4) cauchy
  1) baart
                                                             8) clement
  5) chebspec
                     6) chow
                                         7) circul
  9) companion
                    10) deriv2
                                       11) dingdong
                                                            12) fiedler
 13) forsythe
                    14) foxgood
                                        15) frank
                                                            16) golub
                                        19) hadamard
  17) gravity
                     18) grcar
                                                            20) hankel
 21) heat
                     22) hilb
                                        23) invhilb
                                                            24) invol
 25) kahan
                     26) kms
                                        27) lehmer
                                                            28) lotkin
                    30) minij
                                       31) moler
                                                            32) neumann
 29) magic
 33) oscillate
                   34) parter
                                        35) pascal
                                                            36) pei
 37) phillips
                                                            40) randcorr
                   38) poisson
                                        39) prolate
 41) rando
                    42) randsvd
                                        43) rohess
                                                            44) rosser
 45) sampling
                                        47) spikes
                     46) shaw
                                                            48) toeplitz
 49) tridiag
                     50) triw
                                        51) ursell
                                                            52) vand
 53) wathen
                     54) wilkinson
                                        55) wing
Groups:
  all
               data
                             eigen
                                          ill-cond
               pos-def
  inverse
                             random
                                          regprob
  sparse
               symmetric
```

All the matrices and groups in the collection are shown. It is also possible to obtain just the list of matrix names.

```
> matrixdepot("all")
55-element Array {ASCIIString,1}:
 "baart"
 "binomial"
 "blur"
 "cauchy"
 "chebspec"
 "chow"
 "circul"
 "clement"
 "spikes"
 "toeplitz"
 "tridiag"
 "triw"
 "ursell"
 "vand"
 "wathen"
 "wilkinson"
 "wing"
```

Here, "..." denotes that we have omitted some of the output in order to save space. Next, we check the input options of the Hilbert matrix hilb.

```
Input options:
    * [type,] dim: the dimension of the matrix.
    * [type,] row_dim, col_dim: the row and column dimensions.

Groups: ["inverse", "ill-cond", "symmetric", "pos-def"]

References:

M. D. Choi, Tricks or treats with the Hilbert matrix, Amer. Math. Monthly, 90 (1983), pp. 301-312.

N. J. Higham, Accuracy and Stability of Numerical Algorithms, second edition, Society for Industrial and Applied Mathematics, Philadelphia, PA, USA, 2002; sec. 28.1.
```

Note that an optional first argument type can be given; it defaults to Float64. The string of equals signs on the third line in the output above is Markdown notation for a header. Julia interprets Markdown within documentation, though as we are using typewriter font for code examples here, we display the uninterpreted source. We generate a  $4 \times 6$  Hilbert matrix with elements in the default double precision type and then in Rational type.

```
> matrixdepot("hilb", 4, 6)
4x6 Array{Float64,2}:
 1.0
          0.5
                   0.333333 0.25
                                        0.2
                                                  0.166667
          0.333333 0.25
0.5
                              0.2
                                        0.166667
                                                 0.142857
0.333333 0.25 0.2
                              0.166667
                                        0.142857
                                                 0.125
0.25
          0.2
                   0.166667 0.142857
                                        0.125
                                                  0.111111
> matrixdepot("hilb", Rational, 4, 6)
4x6 Array{Rational{T<:Integer},2}:
      1//2
           1//3
                 1//4
                        1//5
 1//1
                             1//6
                 1//5
 1//2
      1//3
           1//4
                        1//6 1//7
      1//4
           1//5
 1//3
                 1//6
                       1//7
                             1//8
 1//4
      1//5
            1//6
                 1//7 1//8
                              1//9
```

A list of all the symmetric matrices in the collection is readily obtained.

```
> matrixdepot("symmetric")
21-element Array{ASCIIString,1}:
    "cauchy"
    "circul"
    "clement"
    "dingdong"
    "fiedler"
    "hankel"
    "hilb"
    "invhilb"
    "kms"
    "lehmer"
    "minij"
    "moler"
    "oscillate"
```

```
"pascal"
"pei"
"poisson"
"prolate"
"randcorr"
"tridiag"
"wathen"
"wilkinson"
```

Here, symmetric is one of several predefined groups, and multiple groups can be intersected. For example, the for loop below prints the smallest and largest eigenvalues of all the  $4 \times 4$  matrices in Matrix Depot that are symmetric positive definite and (potentially) ill conditioned.

```
> for name in matrixdepot("symmetric", "pos-def", "ill-cond")
    A = full(matrixdepot(name, 4))
    @printf "%9s: smallest eigval = %0.3e, largest eigval = %0.3e\n"
    name eigmin(A) eigmax(A)
end

cauchy: smallest eigval = 2.131e-05, largest eigval = 9.776e-01
    hilb: smallest eigval = 9.670e-05, largest eigval = 1.500e+00
    invhilb: smallest eigval = 6.666e-01, largest eigval = 1.034e+04
    kms: smallest eigval = 3.750e-01, largest eigval = 2.086e+00
    moler: smallest eigval = 3.336e-02, largest eigval = 5.122e+00
oscillate: smallest eigval = 1.490e-08, largest eigval = 1.000e+00
    pascal: smallest eigval = 3.802e-02, largest eigval = 2.630e+01
    pei: smallest eigval = 1.000e+00, largest eigval = 5.000e+00
tridiag: smallest eigval = 3.820e-01, largest eigval = 3.618e+00
```

Matrices can also be accessed by number within the alphabetical list of matrix names.

```
> matrixdepot(2)
"binomial"
> matrixdepot(2:5)
4-element Array {ASCIIString,1}:
 "binomial"
 "cauchy"
 "chebspec"
 "chow"
> matrixdepot(15:20, 5, 6, 1:3)
11-element Array{AbstractString,1}:
 "frank"
 "golub"
 "gravity"
 "grcar"
 "hadamard"
 "hankel"
 "chebspec"
 "chow"
 "baart"
 "binomial"
 "blur"
```

Access by number provides a convenient way to run a test on subsets of matrices in the collection. However, the number assigned to a matrix may change if we include new matrices in the collection. In order to run tests in a way that is repeatable in the future it is best to group matrices into subsets using the macro <code>@addgroup</code>. For example, the following command will group test matrices <code>frank</code>, <code>golub</code>, <code>gravity</code>, <code>grcar</code>, <code>hadamard</code>, <code>hankel</code>, <code>chebspec</code>, <code>chow</code>, <code>baart</code>, <code>binomial</code>, and <code>blur</code> into <code>test1</code>.

```
> @addgroup test1 = matrixdepot(15:20, 5, 6, 1:3)
```

After reloading the package, we can run tests on these matrices using group test1. Since blur (an image deblurring test problem) generates a sparse matrix and the matrix 2-norm is currently not implemented for sparse matrices in Julia, we use full to convert the matrix to dense format.

```
> for name in matrixdepot("test1")
    A = full(matrixdepot(name , 4))
    @printf "%9s has 2-norm %0.3e \n" name norm(A)
end

baart has 2-norm 3.192e+00
binomial has 2-norm 4.576e+00
    blur has 2-norm 8.298e-01
chebspec has 2-norm 6.474e+00
    chow has 2-norm 3.414e+00
    frank has 2-norm 7.624e+00
    golub has 2-norm 2.050e+02
gravity has 2-norm 6.656e+00
    grcar has 2-norm 2.562e+00
hadamard has 2-norm 2.000e+00
hankel has 2-norm 1.160e+01
```

To download the test matrix SNAP/web-Google from the University of Florida sparse matrix collection (see Section 4.3 for more details), we first download the data with

```
> matrixdepot("SNAP/web-Google", :get)
```

and then generate the matrix with

```
> matrixdepot("SNAP/web-Google", :r)
916428x916428 sparse matrix with 5105039 Float64 entries:
        [11343 ,
                    1] =
                            1.0
       [11928 ,
                    1] =
                            1.0
                    1] =
       [15902 ,
                            1.0
       [29547 ,
                    1] =
                           1.0
                    1] = 1.0
        [30282 ,
        [31301 ,
                    1] = 1.0
        [38717 ,
                    1] = 1.0
        [720325, 916427] = 1.0
        [772226, 916427] = 1.0
        [785097, 916427]
                           1.0
        [788476, 916427] = 1.0
        [822938, 916427] = 1.0
        [833616, 916427] = 1.0
        [417498, 916428] =
                           1.0
```

```
[843845, 916428] = 1.0
```

Note that the omission marked "..." was in this case automatically done by Julia based on the height of the terminal window. Matrices loaded in this way are inserted into the list of available matrices, and assigned a number. After downloading further matrices HB/1138\_bus, HB/494\_bus, and Bova/rma10 the list of matrices is as follows.

```
> matrixdepot()
Matrices:
   1) baart
                        2) binomial
                                             3) blur
                                                                  4) cauchy
   5) chebspec
                        6) chow
                                             7) circul
                                                                  8) clement
                       10) deriv2
                                            11) dingdong
                                                                 12) fiedler
   9) companion
  13) forsythe
                       14) foxgood
                                            15) frank
                                                                 16) golub
                                            19) hadamard
                                                                 20) hankel
  17) gravity
                       18) grcar
  21) heat
                       22) hilb
                                            23) invhilb
                                                                 24) invol
                                            27) lehmer
  25) kahan
                       26) kms
                                                                 28) lotkin
  29) magic
                       30) minij
                                            31) moler
                                                                 32) neumann
  33) oscillate
                       34) parter
                                            35) pascal
                                                                 36) pei
                                            39) prolate
                                                                 40) randcorr
  37) phillips
                       38) poisson
                       42) randsvd
                                            43) rohess
  41) rando
                                                                 44) rosser
  45) sampling
                       46) shaw
                                            47) spikes
                                                                 48) toeplitz
  49) tridiag
                       50) triw
                                            51) ursell
                                                                 52) vand
                                                                 56) Bova/rma10
  53) wathen
                       54) wilkinson
                                            55) wing
  57) HB/1138_bus
                       58) HB/494_bus
                                            59) SNAP/web-Google
Groups:
  all
                                              ill-cond
                 data
                                eigen
  inverse
                 pos-def
                               random
                                              regprob
  sparse
                 symmetric
                                test1
```

## 3 Package Design and Implementation

In this section we describe the design and implementation of Matrix Depot, focusing particularly on the novel aspects of exploitation of multiple dispatch, extensibility of the collection, and user-definable grouping of matrices.

## 3.1 Exploiting Multiple Dispatch

Matrix Depot makes use of multiple dispatch in Julia, an object-oriented paradigm in which the selection of a function implementation is based on the types of each argument of the function. The generic function matrixdepot has eight different methods, where each method itself is a function that handles a specific case. This is neater and more convenient than writing eight "case" statements, as is necessary in many other languages.

```
> methods(matrixdepot)
# 8 methods for generic function "matrixdepot":
matrixdepot() ...
matrixdepot(name::AbstractString) ...
matrixdepot(name::AbstractString, method::Symbol) ...
matrixdepot(props::AbstractString...) ...
```

```
matrixdepot(name::AbstractString, args...) ...
matrixdepot(num::Integer) ...
matrixdepot(ur::UnitRange{T<:Real}) ...
matrixdepot(vs::Union{Integer,UnitRange{T<:Real}}...) ...</pre>
```

For example, the following two functions are used for accessing matrices by number and range respectively, where matrix\_name\_list() returns a list of matrix names. The second function calls the first function in the inner loop.

As a result, matrixdepot is a versatile function that can be used for a variety of purposes, including returning matrix information and generating matrices from various input parameters.

In the following example we see how multiple dispatch handles different numbers and types of arguments for the Cauchy matrix.

```
> matrixdepot("cauchy", [1, 2, 3], [4, 5, 6])
3x3 Array{Float64,2}:
0.2
           0.166667 0.142857
           0.142857
 0.166667
                     0.125
 0.142857
           0.125
                     0.111111
> matrixdepot("cauchy", [0.2, 0.3, 0.4])
3x3 Array{Float64,2}:
2.5
          2.0
                   1.66667
          1.66667 1.42857
2.0
1.66667 1.42857 1.25
> matrixdepot("cauchy", 3)
3x3 Array{Float64,2}:
           0.333333 0.25
0.5
 0.333333 0.25
                     0.2
0.25
           0.2
                     0.166667
> matrixdepot("cauchy", Float32, 3)
3x3 Array{Float32,2}:
           0.333333
                     0.25
0.5
 0.333333 0.25
                     0.2
                     0.166667
 0.25
           0.2
```

Multiple dispatch is also exploited in programming the matrices. For example, the Hilbert matrix is implemented as

```
function hilb{T}(::Type{T}, m::Integer, n::Integer)
    H = zeros(T, m, n)
    for j = 1:n, i = 1:m
        @inbounds H[i,j] = one(T)/ (i + j - one(T))
    end
    return H
end
hilb{T}(::Type{T}, n::Integer) = hilb(T, n, n)
hilb(args...) = hilb(Float64, args...)
```

The function hilb has three methods, which enable one to request, for example, hilb(4,2) for a  $4 \times 2$  Hilbert matrix of type Float64, or simply (thanks to the final two lines) hilb(4) for a  $4 \times 4$  Hilbert matrix of type Float64. The keyword @inbounds tells Julia to turn off bounds checking in the following expression, in order to speed up execution. Note that in Julia it is not necessary to vectorize code to achieve good performance [3].

All the matrices in Matrix Depot can be generated using the function call

```
matrixdepot("matrix_name", p1, p2, ...),
```

where matrix\_name is the name of the test matrix, and p1, p2, ..., are input arguments depending on matrix\_name. The help comments for each matrix can be viewed by calling function matrixdepot("matrix\_name"). We can access the list of matrix names by number, range, or a mixture of numbers and range.

1. matrixdepot(i) returns the name of the *i*th matrix;

- 2. matrixdepot(i:j) returns the names of the *i*th to *j*th matrices, where i < j;
- 3. matrixdepot(i:j, k, m) returns the names of the ith, (i + 1)st, ..., jth, kth, and mth matrices.

### 3.2 Matrix Representation

Matrix names in Matrix Depot are represented by Julia strings. For example, the Cauchy matrix is represented by "cauchy". Matrix names and matrix groups are stored as hash tables (Dict). In particular, there is a hash table matrixdict that maps each matrix name to its underlying function and a hash table matrixclass that maps each group to its members.

The majority of parametrized matrices are dense matrices of type Array{T,2}, where T is the element type of the matrix. Variables of the Array type are stored in column-major order. A few matrices are stored as sparse matrices (see also matrixdepot("sparse")), in the Compressed Sparse Column (CSC) format; these include neumann (a singular matrix from the discrete Neumann problem) and poisson (a block tridiagonal matrix from Poisson's equation). Tridiagonal matrices are stored in the built-in type Tridiagonal which is defined as follows.

```
immutable Tridiagonal{T} <: AbstractMatrix{T}
    dl::Vector{T}  # sub-diagonal
    d::Vector{T}  # diagonal
    du::Vector{T}  # sup-diagonal
    du2::Vector{T}  # sup-diagonal
    du2::Vector{T}  # supsup-diagonal for pivoting
end</pre>
```

## 3.3 Matrix Groups

A group is a subset of matrices in Matrix Depot. There are ten predefined groups, which are described in Table 1. Each group is represented by a string. For example, the group of random matrices is represented by "random". Matrices can be accessed by group names, as was illustrated in Section 1.

The macro <code>@addgroup</code> is used to add a new group of matrices to Matrix Depot and the macro <code>@rmgroup</code> removes an added group. All the predefined matrix groups are stored in the hash table <code>matrixclass</code>. The macro <code>@addgroup</code> essentially adds a new key-value combination to the hash table <code>usermatrixclass</code>. Using a separate hash table prevents the user from contaminating the predefined matrix groups.

Being able to create groups is a useful feature for reproducible research [10]. For example, if we have implemented algorithm alg01 and we used circul, minij, and grcar as test matrices for alg01, we could type

```
> @addgroup alg01_group = ["circul", "minij", "grcar"]
```

This adds a new group to Matrix Depot (we need to reload the package to see the changes).

Table 1: Matrix properties.

Group	Description
all	All the matrices in the collection.
data	The matrix has been downloaded from the University of
	Florida Sparse Collection or the Matrix Market Collection.
eigen	Part of the eigensystem of the matrix is explicitly known.
ill-cond	The matrix is ill-conditioned for some parameter values.
inverse	The inverse of the matrix is known explicitly.
pos-def	The matrix is positive definite for some parameter values.
random	The matrix has random entries.
regprob	The output is a test problem for regularization methods.
sparse	The matrix is sparse.
symmetric	The matrix is symmetric for some parameter values.

```
9) deriv2
                      10) dingdong
                                          11) fiedler
                                                               12) forsythe
  13) foxgood
                      14) frank
                                          15) gravity
                                                               16) grcar
                      18) hankel
                                          19) heat
  17) hadamard
                                                               20) hilb
  21) invhilb
                      22) invol
                                          23) kahan
                                                               24) kms
  25) lehmer
                      26) lotkin
                                          27) magic
                                                               28) minij
  29) moler
                      30) neumann
                                          31) oscillate
                                                               32) parter
  33) pascal
                      34) pei
                                          35) phillips
                                                               36) poisson
  37) prolate
                      38) randcorr
                                          39) rando
                                                               40) randsvd
  41) rohess
                      42) rosser
                                          43) sampling
                                                               44) shaw
                     46) tridiag
                                                               48) vand
  45) toeplitz
                                          47) triw
  49) wathen
                      50) wilkinson
                                          51) wing
                                                               52) Bova/rma10
  53) HB/1138_bus
                      54) HB/494_bus
                                          55) SNAP/web-Google
Groups:
  all
                data
                              eigen
                                            ill-cond
  inverse
                pos-def
                              random
                                            regprob
  sparse
                symmetric
                              alg01_group
```

We can then run algo1 on the test matrices by

```
> for name in matrixdepot(alg01_group)
   A = matrixdepot(name, n) # n is the dimension of the matrix.
   @printf "Test result for %9s is %0.3e" name alg01(A)
end
```

## 3.4 Adding New Matrix Generators

Generators are Julia functions that generate test matrices. When Matrix Depot is first loaded, a directory myMatrixDepot is created. It contains two files, group.jl and generator.jl, where group.jl is used for storing all the user defined groups (see Section 3.3) and generator.jl is used for storing generator declarations.

Julia packages are simply Git repositories<sup>1</sup>. The directory myMatrixDepot is untracked by Git,

<sup>&</sup>lt;sup>1</sup>Git is a free and open source distributed version control system.

so any local changes to files in myMatrixDepot do not make the MatrixDepot package "dirty". In particular, all the newly defined groups or matrix generators will not be affected when we upgrade to a new version of Matrix Depot. Matrix Depot automatically loads all Julia files in myMatrixDepot. This feature allows a user to simply drop generator files into myMatrixDepot without worrying about how to link them to Matrix Depot.

A new generator is declared using the syntax include\_generator(FunctionName, "fname", f). This adds the new mapping "fname"  $\rightarrow$  f to the hash table matrixdict, which we recall maps each matrix name to its underlying function. Matrix Depot will refer to function f using string "fname" so that we can call function f by matrixdepot("fname"...).

For example, suppose we have the following Julia file rand.jl, which contains two generators randsym and randorth and we want to use them from Matrix Depot. The triple quotes in the file delimit the documentation for the functions.

```
random symmetric matrix
Input options:
* n: the dimension of the matrix
function randsym(n)
 A = zeros(n, n)
 for j = 1:n
     for i = 1:j
         A[i,j] = randn()
         if i != j; A[j,i] = A[i,j] end
     end
 end
 return A
end
.....
random orthogonal matrix
Input options:
* n: the dimension of the matrix
randorth(n) = qr(randn(n,n))[1]
```

We can copy the file rand.jl to the directory myMatrixDepot and write the following two lines to generator.jl.

```
include_generator(FunctionName, "randsym", randsym)
include_generator(FunctionName, "randorth", randorth)
```

This includes the functions randsym and randorth in Matrix Depot, as we can see by looking at the matrix list.

```
> matrixdepot()
```

```
Matrices:
                                       3) blur
  1) baart
                     2) binomial
                                                              4) cauchy
                     6) chow
  5) chebspec
                                          7) circul
                                                              8) clement
                                        11) dingdong
                                                              12) fiedler
  9) companion
                    10) deriv2
                                       15) frank
19) hadamard
23) invhilb
27) lehmer
31) moler
35) pascal
39) prolate
43) randsvd
                    14) foxgood
  13) forsythe
                                                              16) golub
                    18) grcar
                                                              20) hankel
  17) gravity
  21) heat
                     22) hilb
                                                              24) invol
  25) kahan
                    26) kms
                                                             28) lotkin
                    30) minij
  29) magic
                                                             32) neumann
                  34) parter
38) poisson
  33) oscillate
                                                             36) pei
                                                             40) randcorr
  37) phillips
  41) rando
                    42) randorth
                                                             44) randsym
                                        47) sampling
                    46) rosser
  45) rohess
                                                             48) shaw
                    50) toeplitz
                                        51) tridiag
  49) spikes
                                                             52) triw
 53) ursell
                                         55) wathen
                    54) vand
                                                             56) wilkinson
  57) wing
Groups:
  all
               data
                              eigen
                                            ill-cond
                             random
  inverse
              pos-def
                                          regprob
               symmetric
  sparse
```

The new generators can be used just like the built-in ones.

```
> matrixdepot("randsym")
   random symmetric matrix
    Input options:
    * n: the dimension of the matrix
> matrixdepot("randsym", 4)
4x4 Array{Float64,2}:
-0.765096
 0.174531 1.69308
                   0.269062 0.594058
         0.269062 -0.824277 -0.541458
-1.73322
-0.765096 0.594058 -0.541458 -0.480428
> matrixdepot("randorth")
   random orthogonal matrix
    Input options:
    * n: the dimension of the matrix
> A = matrixdepot("randorth", 4)
4x4 Array {Float64,2}:
-0.769649 -0.141938 -0.5807
                           -0.224235
 0.247165 0.832118 -0.449941 -0.20986
-0.540204 0.505046 0.377263 0.557477
> A'*A - eye(4,4)
4x4 Array{Float64,2}:
-2.22045e-16 1.66533e-16 -2.77556e-17 -1.66533e-16
```

```
1.66533e-16 -1.11022e-16 -3.05311e-16 1.66533e-16
-2.77556e-17 -3.05311e-16 -1.11022e-16 1.94289e-16
-1.66533e-16 1.66533e-16 1.94289e-16 0.0
```

We can also add group information with the function include\_generator. The following lines are put in generator.jl.

```
include_generator(Group, "random", randsym)
include_generator(Group, "random", randorth)
```

This adds the functions randsym and randorth to the group random, as we can see with the following query (after reloading the package).

```
> matrixdepot("random")
10-element Array{ASCIIString,1}:
    "golub"
    "oscillate"
    "randcorr"
    "rando"
    "randorth"
    "randsvd"
    "randsym"
    "rohess"
    "rosser"
    "wathen"
```

#### 3.5 Documentation

The Matrix Depot documentation is created using the documentation generator Sphinx<sup>2</sup> and is hosted at Read the Docs<sup>3</sup>. Its primary goals are to provide examples of usage of Matrix Depot and to give a brief summary of each matrix in the collection. Matrices are listed alphabetically with hyperlinks to the documentation for each matrix. Most parametrized matrices are presented with heat map plots, which are produced using the Winston package<sup>4</sup>, with the color range determined by the smallest and largest entries of the matrix. For example, Figure 1 shows how the Wathen matrix is documented in Matrix Depot.

#### 4 The Matrices

We now describe the matrices that are provided with, or can be downloaded into, Matrix Depot.

#### 4.1 Parametrized Matrices

In Matrix Depot v0.5.2, there are 55 parametrized matrices (including the regularization problems described in the next section), most of which originate from the Test Matrix Toolbox [21]. All these matrices can be generated as matrixdepot("matrix\_name", n), where n is the dimension of the matrix.

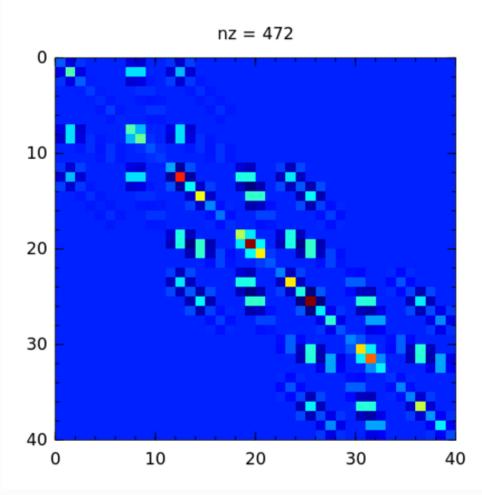
```
2http://sphinx-doc.org/
```

<sup>&</sup>lt;sup>3</sup>http://matrixdepotjl.readthedocs.org

<sup>4</sup>https://github.com/nolta/Winston.jl

#### wathen

The Wathen matrix is a sparse, symmetric positive, random matrix arising from the finite element method [wath87]. It is the consistent mass matrix for a regular *nx-by-ny* grid of 8-node elements.



[wath87] A.J. Wathen, Realistic eigenvalue bounds for the Galerkin mass matrix, IMA J. Numer. Anal., 7 (1987), pp. 449-457.

Figure 1: Documentation for the Wathen matrix

Many matrices can have more than one input parameter, and multiple dispatch provides a convenient mechanism for taking different actions for different argument types. For example, the tridiag function generates a tridiagonal matrix from vector arguments giving the subdiagonal, diagonal, and superdiagonal vectors, but a tridiagonal Toeplitz matrix can be obtained by supplying scalar arguments that specify the dimension of the matrix, the subdiagonal, the diagonal, and the superdiagonal. If a single, scalar argument n is supplied then an n-by-n tridiagonal Toeplitz matrix with subdiagonal and superdiagonal -1 and diagonal 2 is constructed. This matrix arises in applying central differences to a second derivative operator, and the inverse and the condition number are known explicitly [22, sec. 28.5].

Here is an example of the different usages of tridiag.

```
> matrixdepot("tridiag")
    Tridiagonal Matrix
    =============
  Construct a tridiagonal matrix of type Tridiagonal.
  Input options:
       [type,] v1, v2, v3: v1 and v3 are vectors of subdiagonal and
      superdiagonal elements, respectively, and v2 is a vector of diagonal
      elements.
      [type,] dim, x, y, z: dim is the dimension of the matrix, x, y, z are
      scalars. x and z are the subdiagonal and superdiagonal elements,
      respectively, and y is the diagonal elements.
      [type,] dim: x = -1, y = 2, z = -1. This matrix is also known as the
      second difference matrix.
  Groups: ["inverse", "ill-cond", "pos-def", "eigen"]
  References:
  J. Todd, Basic Numerical Mathematics, Vol. 2: Numerical Algebra, Birkhauser,
  Basel, and Academic Press, New York, 1977, p. 155.
> matrixdepot("tridiag", [2,5,6;], ones(4), [3,4,1;])
4x4 Tridiagonal{Float64}:
1.0
     3.0 0.0
               0.0
2.0
     1.0
          4.0
               0.0
0.0
     5.0
          1.0
               1.0
0.0
     0.0
          6.0
               1.0
> matrixdepot("tridiag", 4, 5, 3, 1)
4x4 Tridiagonal{Float64}:
3.0
     1.0
          0.0
               0.0
     3.0
          1.0
5.0
               0.0
0.0
     5.0
          3.0
               1.0
0.0
     0.0
          5.0
               3.0
> matrixdepot("tridiag", Int, 4)
4x4 Tridiagonal{Int64}:
  2 -1
         0
```

#### 4.2 Test Problems for Regularization Methods

A mathematical problem is ill-posed if the solution is not unique or if an arbitrarily small perturbation of the data can cause an arbitrarily large change in the solution. Regularization methods are an important class of methods for dealing with such problems [16], [19]. One means of generating test problems for regularization methods is to discretize a given ill-posed problem.

Matrix Depot contains a group of regularization test problems derived from Hansen's MATLAB Regularization Tools [15], [17], [18] that are mostly discretizations of Fredholm integral equations of the first kind:

$$\int_0^1 K(s,t)f(t) \, dt = g(s), \qquad 0 \le s \le 1.$$

The regularization test problems form the group regprob.

```
> matrixdepot("regprob")
11-element Array{ASCIIString,1}:
    "baart"
    "blur"
    "deriv2"
    "foxgood"
    "gravity"
    "heat"
    "phillips"
    "shaw"
    "spikes"
    "ursell"
    "wing"
```

Each problem is a linear system Ax = b where the matrix A and vectors x and b are obtained by discretization (using quadrature or the Galerkin method) of K, f, and g. By default, we generate only A, which is an ill-conditioned matrix. The whole test problem will be generated if the parameter matrixonly is set to false, and in this case the output has type RegProb, which is defined as

```
immutable RegProb{T}
  A::AbstractMatrix{T}  # matrix of interest
  b::AbstractVector{T}  # right-hand side
  x::AbstractVector{T}  # the solution to Ax = b
end
```

If r is a generated test problem, then r.A, r.b, and r.x are the matrix A and vector x and b respectively. For example, the test problem wing can be generated as follows.

```
* [type,] n, t1, t2, [matrixonly]: the dimension of matrix is n. t1 and
      t2 are two real scalars such that 0 < t1 < t2 < 1. If matrixonly =
      false, the linear system A, b, x will be generated (matrixonly = true
      by default).
      [type,] n, [matrixonly]: t1 = 1/3 and t2 = 2/3.
  Groups: ["regprob"]
  References:
  G. M. Wing, A Primer on Integral Equations of the First Kind, Society for
  Industrial and Applied Mathematics, 1991, p. 109.
> A = matrixdepot("wing", 4)
4x4 Array{Float64,2}:
 0.031189
            0.0921165
                       0.148804
                                 0.198786
0.0310674
            0.0889342
                       0.134959
                                 0.164156
0.0309463
            0.085862
                       0.122403
                                 0.13556
0.0308257
            0.0828958 0.111014
                                 0.111945
> r = matrixdepot("wing", 4, false)
Test problems for Regularization Methods
4x4 Array{Float64,2}:
0.031189
            0.0921165
                       0.148804
                                 0.198786
0.0310674
            0.0889342
                       0.134959
                                 0.164156
0.0309463 0.085862
                       0.122403
                                 0.13556
0.0308257 0.0828958 0.111014 0.111945
4-element Array {Float64,1}:
0.0804953
0.0751385
0.0701787
0.0655842
4-element Array {Float64,1}:
0.0
0.5
0.5
0.0
> r.x
4-element Array{Float64,1}:
0.0
0.5
 0.5
 0.0
```

#### 4.3 Matrix Data from External Sources

Matrix Depot provides access to matrices from Matrix Market [5] and the University of Florida Sparse Matrix Collection [8], [9], both of which contain many matrices taken from applications.

In particular, these sources contain many large, sparse matrices.

Matrix Market and the University of Florida Sparse Matrix Collection both categorize matrices by application domain and the problem source and both provide matrices in Matrix Market Format [6]. These similarities allow us to design a generic interface for both collections. The symbol :get (or :g) is used for downloading matrices from both collections and the symbol :read (or :r) is used for reading in matrices already downloaded. Downloaded matrix data is stored on disk in the Matrix Market format and when read into Julia is stored in the type SparseMatrixCSC.

MatrixDepot.update() downloads the matrix name data files from the two web servers.

```
> MatrixDepot.update()
              % Received % Xferd
  % Total
                                    Average Speed
                                                      Time
                                                               Time
                                                                        Time
                                                                               Current
                                    Dload
                                            Upload
                                                      Total
                                                               Spent
                                                                        Left
                                                                               Speed
100 1887k
              0 1887k
                                                                                 472k
                          0
                                 0
                                    97337
                                                0 --:--
                                                             0:00:19
  % Total
              % Received % Xferd
                                                               Time
                                    Average Speed
                                                      Time
                                                                        Time
                                                                               Current
                                    Dload
                                            Upload
                                                      Total
                                                               Spent
                                                                               Speed
100 41552
              0 41552
                          0
                                 0
                                     4421
                                                0 --:--
                                                             0:00:09
                                                                                41018
```

The UF Sparse Matrix Collection is divided into matrix groups and the group of a matrix forms part of the full name of the matrix [9]. For example, the full name of the matrix 1138\_bus in the Harwell-Boeing Collection is HB/1138\_bus.

```
> matrixdepot("HB/1138_bus", :get)
  % Total
               % Received % Xferd
                                       Average Speed
                                                                               Time
                                                          Time
                                                                    Time
                                                                                      Current
                                       Dload
                                                Upload
                                                          Total
                                                                    Spent
                                                                               Left
                                                                                      Speed
100 19829
             100 19829
                             0
                                        2320
                                                        0:00:08
                                                                   0:00:08 --:-- 49572
> matrixdepot("HB/1138_bus", :read)
1138x1138 Symmetric {Float64, SparseMatrixCSC {Float64, Int64}}:
 1474.78
                0.0
                            0.0
                                           0.0
                                                       0.0
                                                                              0.0
                                                                     0.0
     0.0
                9.13665
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
    0.0
                0.0
                           69.6147
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
    0.0
                0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
    -9.01713
                0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
                0.0
                                                                              0.0
    0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                    . . .
    0.0
                0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
     0.0
                0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
                0.0
                                           0.0
                                                       0.0
     0.0
                            0.0
                                                                     0.0
                                                                              0.0
                -3.40599
    0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
     . . .
                                                                              . . .
                0.0
    0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
                0.0
                                                     -24.3902
     0.0
                            0.0
                                           0.0
                                                                     0.0
                                                                              0.0
     0.0
                0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
     0.0
                 0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
     0.0
                 0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                              0.0
     0.0
                0.0
                            0.0
                                          26.5639
                                                       0.0
                                                                     0.0
                                                                              0.0
     0.0
                0.0
                            0.0
                                           0.0
                                                      46.1767
                                                                     0.0
                                                                              0.0
     0.0
                0.0
                             0.0
                                           0.0
                                                       0.0
                                                                 10000.0
                                                                              0.0
     0.0
                0.0
                            0.0
                                           0.0
                                                       0.0
                                                                     0.0
                                                                           117.647
```

Matrices from the University of Florida Sparse Matrix Collection are stored in MatrixDepot/data/uf and they are stored by group (to avoid duplicate names), i.e., one directory per group. Similarly, matrices from Matrix Market are stored in MatrixDepot/data/mm. Both directories are untracked by Git.

We can download a whole group of matrices from the University of Florida sparse matrix collection using the command matrixdepot("group name/\*", :get). The next example downloads all 67 matrices in the Gset group of matrices from random graphs (contributed by Y. Ye) then displays all the matrices in Matrix Depot, including the newly downloaded matrices.

```
> matrixdepot("Gset/*", :get)
Downloading all matrices in group Gset...
             % Received % Xferd
                                 Average Speed
                                                 Time
                                                         Time
                                                                  Time
                                                                         Current
                                 Dload Upload
                                                 Total
                                                         Spent
                                                                  Left
                                                                         Speed
           100 48083
                        0
                                 95388
                                            0 --:--: 96166
download:/home/weijian/.julia/v0.4/MatrixDepot/src/../data/uf/Gset/G1.tar.gz
G1/G1.mtx
             % Received % Xferd
 % Total
                                 Average Speed
                                                 Time
                                                         Time
                                                                  Time
                                                                         Current
                                 Dload Upload
                                                 Total
                                                         Spent
                                                                  Left
                                                                         Speed
100 55180
          100 55180
                        0
                              0
                                            0 --:--: 75692
                                 75318
download:/home/weijian/.julia/v0.4/MatrixDepot/src/../data/uf/Gset/G10.tar.gz
G10/G10.mtx
  % Total
             % Received % Xferd
                                 Average Speed
                                                 Time
                                                         Time
                                                                  Time
                                                                         Current
                                 Dload Upload
                                                 Total
                                                         Spent
                                                                  Left
                                                                         Speed
100 5926
           100 5926
                        0
                              0
                                 23126
                                            0 --:--: 23515
download:/home/weijian/.julia/v0.4/MatrixDepot/src/../data/uf/Gset/G11.tar.gz
G11/G11.mtx
  % Total
             % Received % Xferd
                                 Average Speed
                                                         Time
                                 Dload Upload
                                                 Total
                                                         Spent
                                                                  Left
                                                                         Speed
100
     6349
           100
                6349
                                 24223
                                            0 --:--: 24608
> matrixdepot()
Matrices:
   1) baart
                       2) binomial
                                           3) blur
                                                               4) cauchy
                                           7) circul
   5) chebspec
                       6) chow
                                                               8) clement
                      10) deriv2
   9) companion
                                          11) dingdong
                                                              12) fiedler
  13) forsythe
                      14) foxgood
                                          15) frank
                                                              16) golub
  17) gravity
                      18) grcar
                                          19) hadamard
                                                              20) hankel
                      22) hilb
  21) heat
                                          23) invhilb
                                                              24) invol
  25) kahan
                      26) kms
                                          27) lehmer
                                                              28) lotkin
  29) magic
                      30) minij
                                          31) moler
                                                              32) neumann
  33) oscillate
                      34) parter
                                          35) pascal
                                                              36) pei
  37) phillips
                      38) poisson
                                          39) prolate
                                                              40) randcorr
                                                              44) rosser
  41) rando
                      42) randsvd
                                          43) rohess
  45) sampling
                      46) shaw
                                          47) spikes
                                                              48) toeplitz
  49) tridiag
                      50) triw
                                          51) ursell
                                                              52) vand
  53) wathen
                      54) wilkinson
                                          55) wing
                                                              56) Gset/G10
  57) Gset/G11
                      58) Gset/G12
                                          59) Gset/G13
                                                              60) Gset/G14
                      62) Gset/G16
                                          63) Gset/G17
                                                              64) Gset/G18
  61) Gset/G15
                      66) Gset/G1
  65) Gset/G19
                                          67) Gset/G20
                                                              68) Gset/G21
  69) Gset/G22
                      70) Gset/G23
                                          71) Gset/G24
                                                              72) Gset/G25
  73) Gset/G26
                      74) Gset/G27
                                          75) Gset/G28
                                                              76) Gset/G29
  77) Gset/G2
                      78) Gset/G30
                                          79) Gset/G31
                                                              80) Gset/G32
  81) Gset/G33
                      82) Gset/G34
                                          83) Gset/G35
                                                              84) Gset/G36
  85) Gset/G37
                      86) Gset/G38
                                          87) Gset/G39
                                                              88) Gset/G3
  89) Gset/G40
                      90) Gset/G41
                                          91) Gset/G42
                                                              92) Gset/G43
  93) Gset/G44
                      94) Gset/G45
                                          95) Gset/G46
                                                              96) Gset/G47
  97) Gset/G48
                      98) Gset/G49
                                          99) Gset/G4
                                                             100) Gset/G50
```

```
101) Gset/G51
                      102) Gset/G52
                                            103) Gset/G53
                                                                  104) Gset/G54
 105) Gset/G55
                      106) Gset/G56
                                            107) Gset/G57
                                                                  108) Gset/G58
 109) Gset/G59
                      110) Gset/G5
                                            111) Gset/G60
                                                                  112) Gset/G61
 113) Gset/G62
                      114) Gset/G63
                                            115) Gset/G64
                                                                  116) Gset/G65
 117) Gset/G66
                      118) Gset/G67
                                            119) Gset/G6
                                                                  120) Gset/G7
                      122) Gset/G9
 121) Gset/G8
Groups:
  all
                                               ill-cond
                 data
                                eigen
  inverse
                 pos-def
                                random
                                               regprob
                                test1
  sparse
                 symmetric
```

The full name of a matrix in Matrix Market comprises three parts: the collection name, the set name, and the matrix name. For example, the full name of the matrix BCSSTK14 in the set BCSSTRUC2 from the Harwell-Boeing Collection is Harwell-Boeing/bcsstruc2/bcsstk14. Note that both set name and matrix name are in lower case.

```
> matrixdepot("Harwell-Boeing/bcsstruc2/bcsstk14", :get)
  % Total
              % Received % Xferd
                                    Average Speed
                                                      Time
                                                                         Time
                                                                                Current
                                                               Time
                                    Dload
                                            Upload
                                                      Total
                                                               Spent
                                                                         Left
                                                                                Speed
            100
                 292k
                          0
                                    22635
                                                 0
                                                    0:00:13
                                                              0:00:13 --:-- 61144
download:/home/weijian/.julia/v0.4/MatrixDepot/data/mm/Harwell-Boeing/bcsstruc2
/bcsstk14.mtx.gz
> matrixdepot("Harwell-Boeing/bcsstruc2/bcsstk14", :read)
1806x1806 Symmetric{Float64,SparseMatrixCSC{Float64,Int64}}:
                            -1.02166e5
      1.93161e6
                  0.0
                                                   0.0
                                                                     0.0
      0.0
                   1.0
                             0.0
                                                   0.0
                                                                     0.0
      -1.02166e5
                  0.0
                             1.93147e6
                                                   0.0
                                                                     0.0
 -35568.9
                  0.0
                             1.65787e5
                                                   0.0
                                                                     0.0
      -1.06959e5
                  0.0
                            -1.06959e5
                                                   0.0
                                                                     0.0
      -1.65835e5
                  0.0
                        35568.9
                                                   0.0
                                                                     0.0
   -717.845
                   0.0
                            0.0
                                                   0.0
                                                                     0.0
      0.0
                   0.0
                        88998.5
                                                   0.0
                                                                     0.0
      0.0
                            -1.82865e6
                                                   0.0
                                                                     0.0
                   0.0
      0.0
                   0.0
                             1.24988e5
                                                   0.0
                                                                     0.0
       . . .
                   0.0
                             0.0
                                                   0.0
                                                                     0.0
      0.0
      0.0
                   0.0
                             0.0
                                                   1.06103e7
                                                                    -5.25151e5
                   0.0
                             0.0
      0.0
                                                  -5.25151e5
                                                                -53434.0
      0.0
                   0.0
                             0.0
                                                   1.06959e5
                                                                    -1.65835e5
      0.0
                   0.0
                             0.0
                                                   0.0
                                                                     0.0
      0.0
                   0.0
                             0.0
                                                   1.06959e5
                                                                35568.9
      0.0
                   0.0
                             0.0
                                            -816518.0
                                                                     1.21311e7
      0.0
                             0.0
                                                   4.55624e7
                                                                     8.15266e5
                   0.0
                             0.0
                                                   8.15266e5
                                                                     5.27942e8
      0.0
                   0.0
```

We recommend downloading matrices from the University of Florida sparse matrix collection when there is a choice, because almost every matrix from Matrix Market is included in it.

## 5 Concluding Remarks

Matrix Depot follows in the footsteps of earlier collections of matrices. Its novelty is threefold. First, it is extensible by the user, and so can be adapted to the user's needs. In doing so it facilitates experimentation, and in particular makes it easier to do reproducible research. Second, it

combines three distinct test matrix collections, namely, parametrized test matrices, regularization test problems, and real-life sparse matrix data, in a single framework. Third, it fully exploits the Julia language. It uses multiple dispatch to help provide a simple interface and, in particular, to allow matrices to be generated in any of the numeric data types supported by the language. Matrix Depot therefore anticipates the development of intrinsic support in Julia for computations with BigFloat and other data types.

Matrix Depot has been in development since 2014. It is an open source project<sup>5</sup> hosted on GitHub and is available under the MIT License. A first release was announced in December 2014. Matrix Depot v0.5.2 is the latest official release and consists of around 3,000 lines of source code, with test coverage of 98.91% according to Codecov<sup>6</sup>. From GitHub traffic analytics, we learn that Matrix Depot has 40 to 70 unique downloads (unique cloners) every month. Matrix Depot also benefits the development of other Julia packages. LightGraphs<sup>7</sup>, an optimized graph package for Julia, for example, has embedded Matrix Depot as its database.

We built Matrix Depot to facilitate the development and testing of matrix (and other) algorithms in Julia. and we will continue to develop Matrix Depot by introducing new test matrices and integrating with other test collections.

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 $<sup>^5</sup>$ https://github.com/weijianzhang/MatrixDepot.jl

<sup>6</sup>https://codecov.io/

<sup>&</sup>lt;sup>7</sup>https://github.com/JuliaGraphs/LightGraphs.jl

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